

# Using Electronic Health Records to Monitor and Improve Adherence to Medication

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# Using Electronic Health Records to Monitor and Improve Adherence to Medication

## ABSTRACT

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Adherence to medication is a serious problem in the United States leading to complications and preventable hospitalizations, particularly for patients with chronic diseases. Interventions have been proposed as a means to improve adherence to medication, but the optimal time to perform an intervention has not been well studied. Electronic health records (EHRs) can be used to monitor patient adherence to medication, providing a source of information to help decide when to perform an intervention. We propose a Markov decision process (MDP) model to determine when to perform adherence-improving interventions based on a patient's EHR. We consider the tradeoff between the patient's perspective of maximizing (quality-adjusted) time to first adverse health event and the payer's perspective of minimizing the cost of interventions, medication, and adverse events. We use our model to evaluate the costs and benefits of implementing an EHR-based active surveillance system for adherence-improving interventions in the context of cardiovascular disease management. We also provide some theoretical insights into the structure of the optimal intervention policy and the influence of health risks and costs on intervention decisions.

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*Keywords:* electronic health records; medication adherence; Markov decision process

# 1 Introduction

Poor medication adherence has been estimated to cost approximately \$100 billion per year in preventable hospitalizations in the United States alone (Osterberg and Blaschke [2005]). Recent studies show that while improving adherence results in an increase in medication costs, there are significant overall cost savings, particularly among patients with chronic diseases (Sokol et al. [2005], Ho et al. [2006]). Improved adherence can also reduce the risk of adverse events and improve the quality and length of life for many patients. In spite of the benefits of high adherence, poor adherence is recognized as a major challenge in the medical community (Cutler and Everett [2010]). In 2007 the National Institutes of Health (NIH) implemented the *Adherence Research Network* to promote research on adherence (NIH [2011]). The initiative supports 14 institutes and centers across NIH, highlights NIH funding for adherence research, synthesizes current scientific findings on adherence, and provides leadership on future research directions.

While it is difficult to directly measure the medication taken by patients, there are widely accepted proxy measures of adherence, including patient self reporting, electronic medication monitors on pill canisters, and rates of prescription refills calculated from electronic health records (EHRs). Based on prescription refill estimates of adherence, studies suggest that only 25% of patients remain highly adherent to common treatments such as cholesterol-lowering medication (Benner et al. [2002], Mason et al. [2012]). Adherence-improving interventions, such as collaborative decision making and the use of decision aids to choose medications, have been shown to improve adherence (Weymiller et al. [2007]). However, barriers to such interventions include the perception that they take time and effort and are often not reimbursed by third-party payers. Furthermore, information about an individual patient's adherence to their prescribed medications is normally unavailable to physicians at the time of encounter with a patient.

Recently, considerable attention has been given to the use of EHRs to improve efficiency and effectiveness of healthcare delivery. EHRs are systematic collections of patient health information that can aid physicians in making medical decisions. In the United States, the Centers for Medicare and Medicaid Services (CMS) have recently introduced a *Meaningful Use* initiative (HHS [2011]). The goals of the initiative are to improve safety and efficiency of healthcare delivery through the use of EHRs, and there is over \$20 billion available from the Health Information Technology

1 for Economic and Clinical Health Act (HITECH Act) to promote the adoption of information  
2 technology for healthcare and train skilled workers in this field. Due to incentives created by this  
3 program, healthcare managers are under pressure to meet the objectives of the Meaningful Use  
4 initiative and to submit clinical quality measures (CQMs) using certified EHR technology.

5 EHRs have the potential to enable monitoring of adherence and to identify patients that would  
6 benefit most from an adherence-improving intervention. By actively monitoring patients' adherence  
7 to medications, which we refer to as *active adherence surveillance* (AAS), such decisions could be  
8 made in real time at the point of care. However, implementation of a surveillance system comes at  
9 a cost. Therefore in this article we aim to answer the following research question: What are the  
10 potential benefits of using EHRs to improve adherence to medication? To answer this question,  
11 we use pharmacy claims data for a large population to estimate patient adherence levels to the  
12 most commonly-used medication for cholesterol control. We present a Markov decision process  
13 (MDP) model to determine the optimal timing of adherence-improving interventions based on  
14 AAS of individual patients' adherence using EHRs. Our model considers both the perspective of  
15 the patient, who stands to benefit from the prevention of adverse health events related to poor  
16 adherence, and the perspective of the third-party payer (health insurer) that bears the burden of  
17 the cost of interventions, medication, hospitalizations, and follow-up care for adverse events related  
18 to poor adherence. We present structural properties of our model, including conditions under which  
19 a control limit policy exists, and how the control limit policy changes based on a patient's health  
20 status and the effectiveness of an intervention.

21 There are many prescription medications for which poor adherence is recognized as a challenge  
22 in preventing the onset or progression of disease (e.g., blood pressure control medications, asthma  
23 medications). In this article we provide a specific example based on adherence to *statins*, the  
24 most common cholesterol-lowering medication. We evaluate the costs and benefits associated with  
25 AAS by using our MDP model to determine the following: (a) the expected quality-adjusted life  
26 years (QALYs) before a stroke, a coronary heart disease (CHD) event (such as a heart attack),  
27 or death; and (b) medication and intervention costs and costs associated with the occurrence of  
28 strokes and CHD events (the most significant outcomes associated with cholesterol control). To  
29 estimate the marginal benefits of implementing the EHR-based system, we compare AAS to a

1 much simpler, and easier to implement, schedule of interventions at regularly-spaced intervals (e.g.,  
2 yearly interventions) which we refer to as *inactive adherence surveillance* (IAS). We also compare  
3 our results to outcomes for patients who receive no interventions. In addition, we estimate the  
4 potential yearly benefits of applying AAS to the U.S. population.

5 Our findings have the potential to influence several different stakeholders. First, our findings  
6 will help inform CMS about the potential benefits of AAS, and whether such implementations  
7 should be added to the list of objectives for their Meaningful Use or other future initiatives. Un-  
8 derstanding and improving medication adherence is a natural extension to the current Meaningful  
9 Use requirement of *medical reconciliation*, which requires an accurate list of medications the pa-  
10 tient is currently taking. Second, our results will help inform third-party health insurers about  
11 the potential benefits of reimbursing healthcare providers for adherence-improving interventions.  
12 Third, physicians will benefit from an improved understanding of the relative benefits of address-  
13 ing adherence to medications for chronic conditions. Finally, patients could directly benefit from  
14 improved quality of life and the lower costs that can be achieved by improved adherence.

15 The remainder of this article is organized as follows. In Section 2 we provide some background  
16 on adherence interventions and methods for estimating adherence from EHRs. We also provide  
17 a specific example that illustrates measurement of adherence to statins and its relationship to  
18 health outcomes. In Section 3 we present an overview of related literature in the areas of machine  
19 maintenance and medical decision making. In Section 4 we present our MDP model for determining  
20 the optimal time for interventions, and in Section 5 we explore some general insights that can be  
21 drawn from our model. In Section 6 we present a case study of cholesterol-lowering treatment to  
22 prevent cardiovascular disease in patients with type 2 diabetes. Finally, in Section 7 we provide  
23 concluding remarks and discuss future research opportunities.

## 24 **2 Background on Medication Adherence**

25 Motivation for understanding adherence to medication is summed up in a quote by C. Everett  
26 Koop, M.D.: “Drugs don’t work in patients who don’t take them.” Osterberg and Blaschke [2005]  
27 cite patient forgetfulness and lack of understanding as possible causes of poor adherence. The  
28 authors describe several types of interventions for improving medical adherence including patient

1 education, increased access to medical care, and improved communication between patients and  
2 physicians. For example, performing screening tests and reviewing a patient's risk of an adverse  
3 health event (e.g., 10-year risk of a stroke or CHD event), or educating a patient about the risk  
4 reduction associated with a particular medication, has been shown to improve patient adherence  
5 (Weymiller et al. [2007]).

6 A common method for measuring patient adherence is to observe the percentage of days covered  
7 (PDC) by prescription refills over time. Prescription refills can be observed from pharmacy claims  
8 data, a portion of administrative claims data generated as a result of a patient's encounter with  
9 the health system. Claims data is an important part of the extended EHR that is collected by  
10 third-party payers for payment purposes. If Meaningful Use program objectives are met, more  
11 than 80% of patients will have pharmacy refills recorded as structured data by the end of 2012.

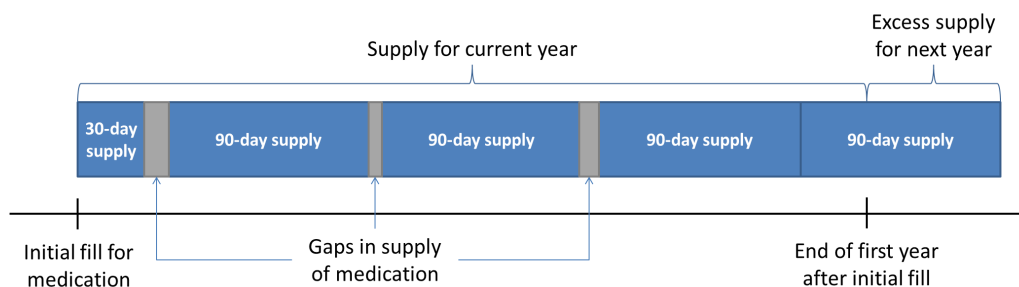
12 The standard formula for PDC is as follows (Caetano et al. [2006]):

$$\text{PDC} = 100 \times \left( \frac{\text{days with an available supply of medication in the time period}}{\text{days in time period}} \right) \%. \quad (1)$$

13 Figure 1 provides an example of a patient's pharmacy claims for which PDC is estimated over a  
14 one-year period. In this example, the patient begins taking the medication with a 30-day supply.  
15 The patient makes four refills, each with 90-day supply, during the year. Gaps between the end of  
16 the days' supply for one prescription fill and the beginning of the next fill are interpreted as gaps in  
17 the patient's adherence to the medication. As shown in Figure 1, refills that have supply exceeding  
18 the amount of time to the end of the year (time period) are carried over to the calculation of the  
19 PDC for the next time period. Note that this method for computing PDC is not restricted by the  
20 days' supply of refills or the refill method (by mail or local pharmacy).

21 Combining pharmacy claims data with laboratory data (e.g., cholesterol, blood sugar, blood  
22 pressure) and other sources of data in the EHR is often necessary to measure the effects of adherence.  
23 For example, the PDC can be linked with the patient's percentage change in metabolic values over  
24 the same time period. We illustrate this with a specific example. Consider the case of patients  
25 initiating statins to lower their cholesterol and therefore lower their risk of stroke and CHD events.

Figure 1: Diagram of Prescription Refills Used to Calculate the Percentage of Days Covered (PDC).



1 States for the PDC over the course of a year after initiation are defined by the four categories given  
 2 in Table 1. The adherence states are defined as follows: NON ( $0 \leq \text{PDC} \leq 10\%$ ), LOW ( $10 <$   
 3  $\text{PDC} \leq 40\%$ ), MED ( $40 < \text{PDC} \leq 80\%$ ), and HIGH ( $80 < \text{PDC} \leq 100\%$ ). These specific choices of  
 4 adherence states are based on those commonly used in the health services research literature (for  
 5 example see Rasmussen et al. [2007]). By using laboratory data, these adherence states are linked  
 6 with changes in total cholesterol (TC) from initiation to one year after initiation. Large data sets  
 7 that combine pharmacy claims data with laboratory data for a large sample of patients can thus  
 8 be used to estimate the expected change in TC for each PDC level.

9 The results in Table 1 are based on a study reported in Mason et al. [2012]. Table 1 establishes  
 10 the link between a patient’s percentage change in TC and her adherence to medication. Since the  
 11 risk of cardiovascular events is affected by TC, the patient’s risk is also correlated with their adher-  
 12 ence to the medication (Kothari et al. [2002], Stevens et al. [2001]). For this reason interventions  
 13 that improve adherence have the potential to reduce cardiovascular risk over time. A method to  
 14 estimate a stochastic model for changes in PDC over time is revisited in Section 6.

Table 1: Adherence States Defined by Percentage of Days Covered (PDC) and the Corresponding Percent Change in Total Cholesterol (TC) for Patients that Initiate Statins.

Adherence State	PDC	Change in TC
NON	0 – 10%	–5.22%
LOW	10 – 40%	–8.21%
MED	40 – 80%	–18.08%
HIGH	80 – 100%	–25.25%

## 3 Literature Review

The problem of finding the optimal time to perform an intervention to improve a patient’s adherence to a medical treatment is analogous to problems studied in the machine maintenance literature. This has been an active area of research for over fifty years. While we do not attempt to fully review this literature, we highlight related articles. In addition to the literature on machine maintenance, we also review articles on the use of the operations research (OR) models and methods for medical decision making.

### 3.1 Machine Maintenance Applications

Pioneering work on maintenance systems was done by Klein [1962], who considers a stochastically deteriorating system that could be replaced or kept after inspection by a manager. If the system was kept, the decision would then be to repair the system or decide the time of the next inspection. The author assumes inspection gives the manager enough information to determine the state of the system. The objective of the model is to minimize the long run average cost of the policy. The model uses a Markov chain to represent probabilistic deterioration of the system. The main difference between Klein’s model and previous machine maintenance models is that the time between successive transitions (inspections) is under the control of the decision maker (manager). This is similar to the model we present in which a decision maker must choose the optimal time for an adherence-improving intervention. The assumption that the manager gains knowledge of the machine’s state through inspection is analogous to a physician gaining knowledge about the patient’s adherence behavior through an office visit.

In McCall [1965], Pierskalla and Voelker [1976], Sherif and Smith [1981], Jardine and Buzacott [1985], Valdez-Flores and Feldman [1989], and Pham and Wang [1996], the authors survey maintenance policies for stochastically failing machines and imperfect repair. The latter in particular is consistent with adherence interventions that have an uncertain outcome, which we consider in this article. In Butler [1979] the authors consider a *hazardous inspection* model in which, similar to adherence intervention, there is potential harm from inspection (e.g., for adherence intervention this could include a monetary cost of intervention or a loss of utility on behalf of the patient). Nakagawa [1988] extends imperfect repair models to a system degrading over time as it ages, similar to the



1 increasing probability of death from other causes in the model we propose. In Armstrong [2002]  
2 the authors extend deterioration models to the case of preemptive maintenance. This is analogous  
3 to the goal of improving a patient’s adherence to reduce the likelihood of future adverse events. All  
4 these studies have similarities to adherence control (albeit in a much different context), but none  
5 combine all the characteristics of the model we propose.

6 Other notable references include the work of Anderson [1981] which presents three continuous-  
7 time MDPs, each with an infinite horizon, continuous state space, and actions for maintenance or  
8 replacement of the machine. The models differ in terms of the rate of deterioration. The models  
9 are transformed into discrete time finite horizon MDPs to prove structural properties that pro-  
10 vide insights on their continuous time counterparts. Anderson provides conditions for each model  
11 for which a control limit structure exists and the preventative maintenance level is nonincreasing.  
12 Hopp and Wu [1990] extend the work of Anderson on a machine maintenance model with preventa-  
13 tive maintenance using an infinite horizon MDP with a finite state space. They prove a control limit  
14 policy and monotonicity. In addition, Hopp and Wu consider the effects of alternate assumptions  
15 on the structural properties they prove for their model. For example, they show the structural  
16 properties still hold when the system must go down for an entire period when maintenance is  
17 performed.

## 18 **3.2 Medical Decision Making Applications**

19 There has been a recent increase in collaboration between the OR community and nonprofit or-  
20 ganizations on the treatment and prevention of HIV/AIDS, including studies to improve adher-  
21 ence to treatment. The Population Council, an international nongovernmental organization, pub-  
22 lished a handbook on designing HIV/AIDS prevention studies using OR methods (Fisher and Foreit  
23 [2002]). The handbook focuses on descriptive models, applying statistical tests and running cost-  
24 effectiveness analysis. The Doris Duke Charitable Foundation has awarded grants recently for the  
25 use of OR methods on AIDS Care and Treatment in Africa (ORACTA) (DDC [2011]). These grants  
26 include funding for studying effectiveness of interventions (e.g., HIV education, text message med-  
27 ication reminders, and home visits by peer educators). This work helps motivate the potential for  
28 prescriptive OR models, such as we discuss in this article, to improve adherence to medication for

1 chronic diseases.

2 MDPs have been used in a number of medical applications for determining when a particular  
3 treatment should start or procedure should take place. For example, Alagoz et al. [2004] consider  
4 the optimal timing of liver transplantation using a live donor in order to maximize the patient's  
5 total reward. The authors use an infinite horizon MDP model to determine the optimal timing  
6 of this one-time decision. Structural properties are derived, including showing the existence of  
7 a control-limit policy under certain assumptions. Shechter et al. [2008] also present an infinite  
8 horizon MDP model to determine the optimal timing of HIV therapy. The states in the model  
9 represent the patient's CD4 count, and the objective is to maximize life years or QALYs over the  
10 patient's lifetime. Results suggest earlier treatment is optimal, contrary to treatment trends at the  
11 time of publication.

12 Maillart et al. [2008] present a partially observable Markov chain model to evaluate various  
13 breast cancer screening policies considering implications of patient adherence to screening guidelines  
14 and differences in breast cancer incidence and aggression as women age. Evaluation, rather than  
15 optimization of policies, is used to selectively compare easy-to-implement policies. Efficient policies  
16 are identified based on the tradeoff between lifetime breast mortality risk and the expected number  
17 of mammograms over a woman's lifetime. Chhatwal et al. [2010] present a finite-horizon discrete-  
18 time MDP to determine the optimal timing of breast biopsy given the outcome of a mammogram  
19 and patient demographic features. The decision epochs are years after age 40, the states represent  
20 the patient's risk score, determined after a mammogram, and the actions are to have a biopsy or  
21 to have another mammogram the following year. Once the action of biopsy is taken, the patient  
22 leaves the decision process. Rewards are defined by QALYs accrued by patients. Chhatwal et al.  
23 prove structural properties for their model, including the existence of a control-limit type policy.  
24 Results suggest that the decision to biopsy should depend on the patient's age.

25 Denton et al. [2009] propose an MDP model to find the optimal time to initiate statins in  
26 patients with type 2 diabetes for the prevention of cardiovascular events. The states represent  
27 the patient's metabolic risk factors. The rewards are monetary rewards for QALYs minus costs of  
28 medication and treatment for cardiovascular events, and the action to initiate or defer initiation of  
29 treatment is revisited each year. The authors consider the effects of using different cardiovascular

1 risk models to estimate the probability of adverse events, concluding that the risk model chosen can  
2 dramatically affect the optimal start times. Their model assumes perfect adherence to treatment.  
3 Mason et al. [2012] propose a related MDP model to find the optimal time to initiate statins given  
4 the possibility of imperfect adherence. The authors incorporate a Markov model for adherence  
5 after the patient begins statins. The authors conclude that timing of initiation does not have as  
6 great of an effect on patient outcomes as improving adherence; however, they note that adherence-  
7 improving interventions can be costly. This study provides motivation for the study of the optimal  
8 time of adherence-improving interventions once treatment has begun.

### 9 **3.3 Contributions of this Article**

10 To our knowledge, the problem of finding the optimal time to perform an intervention to improve  
11 medication adherence has not been studied before. This problem is analogous to problems studied  
12 in the machine maintenance literature; however, there are differences. First, in our model there  
13 is no available action to replace the system; only preventative maintenance may be performed.  
14 Second, we consider a system that is deteriorating in a nonstationary fashion over a finite horizon.  
15 Our model also differs in several ways from the literature on MDP models for medical decision  
16 making described above. First, the decision to initiate an adherence-improving intervention is a  
17 recurring decision and not a one-time decision as considered by Denton et al. [2009], Alagoz et al.  
18 [2004], Chhatwal et al. [2010], and Shechter et al. [2008]. Second, unlike the majority of the above  
19 models, which are infinite-horizon models, our proposed model is finite horizon and nonstationary,  
20 to reflect nonstationarity in the risk of adverse events with respect to a patient's age. Finally,  
21 and most notably, our study is unique in its specific application, in the methods and data used to  
22 estimate the model parameters, and in the research question we propose to answer.

23 As a result of the differences between our model and those previously proposed in the literature,  
24 we make several contributions. We present new structural properties that provide insight into  
25 optimal adherence intervention policies, and motivate easy-to-implement rules of thumb for when  
26 to initiate an intervention. We use a large data set that combines pharmacy claims data with  
27 the laboratory data necessary to construct and solve the MDP model we propose, and we present  
28 results based on this model for a specific example in the context of statin treatment for a population

1 of patients at high risk of stroke and CHD events. To our knowledge, these results are the first  
2 estimates of the potential benefits that may be derived from active surveillance of patient adherence  
3 to medication.

## 4 **4 Model Formulation**

5 In each of a set of discrete decision epochs, a patient on a particular medication is observed to be in  
6 a specific health state. The health states are divided into *adherence states* and an *absorbing state*.  
7 The adherence states represent the patient’s level of adherence to the medication (e.g., statins), and  
8 the absorbing state represents the occurrence of events that the treatment aims to prevent (e.g.,  
9 a stroke or CHD event) or death from other causes. In each decision epoch, the decision maker  
10 (e.g., the physician) must decide whether or not to implement an intervention with the patient.  
11 Thus, one of two possible actions is taken: *implement an intervention* or *defer the decision until*  
12 *the next epoch*. This decision is faced at each decision epoch, provided the patient does not enter  
13 the absorbing state. The following is a detailed description of the MDP model.

14 *Time Horizon:* The decision to initiate an adherence-improving intervention is revisited periodically  
15 over a finite horizon with  $T$  yearly decision epochs. The decision epochs are indexed by  $t =$   
16  $0, 1, 2, \dots, T$  where time epoch  $t$  represents the time interval  $[t, t + 1)$ . Time  $t = 0$  represents the  
17 initial epoch when the patient begins surveillance (the patient begins taking the medication), and  $T$   
18 is chosen as a reasonable upper bound on a typical patient’s age (e.g., 100 years). For patients who  
19 have not entered the absorbing state at time  $T$ , a reward is obtained that estimates the benefits and  
20 costs associated with their future survival, based on an estimate of the patient’s future remaining  
21 life years.

22 *States:* The states of the patient are represented by the set  $S \equiv \{0, 1, 2, \dots, M\}$ ; for each time  
23  $t = 0, \dots, T$ , we let  $s_t \in S \setminus \{0\}$  denote the patient’s adherence level for time epoch  $t$ , while  $s_t = 0$   
24 indicates that the patient had an adverse health event (fatal or nonfatal) or that the patient died  
25 from other causes. For  $s_t \in S \setminus \{0\}$ , a larger value of  $s_t$  corresponds to an increased (improved)  
26 level of adherence for the patient at time  $t$ .

27 *Actions:* An intervention may be initiated or deferred at any epoch,  $t = 1, \dots, T - 1$ , and in any

1 state,  $s_t \in S \setminus \{0\}$ . The possible set of actions is defined as the following:

$$A_t(s_t) = \begin{cases} \{W, I\} & \text{for } s_t \in S \setminus \{0\} \text{ and } t = 1, \dots, T-1, \\ \{W\} & \text{for } s_t = 0 \text{ or } t = T, \end{cases}$$

2 so that  $a_t(s_t) \in A_t(s_t)$  denotes the action taken at time  $t$  when the patient is in state  $s_t$ , where  
 3 the action  $a_t = I$  denotes an intervention and the action  $a_t = W$  denotes the action of waiting, or  
 4 deferring the decision until the next epoch. The total action space is defined by  $A = \{W, I\}$ .

5 *Transition Probabilities:* There are two types of transition probabilities: (a) transitions between  
 6 adherence states; and (b) transitions from adherence states to the absorbing state. Given avoidance  
 7 of state 0, the conditional transition probabilities between the adherence states are represented by  
 8 the matrix  $\tilde{P}_t(a_t) \in \mathbb{R}^{M \times M}$  so that  $[\tilde{P}_t(a_t)]_{i,j}$ , the  $(i, j)$  element of  $\tilde{P}_t(a_t)$ , is equal to the conditional  
 9 probability  $\Pr\{s_{t+1} = j | s_t = i \text{ and } s_{t+1} \neq 0\}$  for  $1 \leq i, j \leq M$ . Transitions from adherence states  
 10 to the absorbing state are represented by the vector  $\bar{p}_t \in \mathbb{R}^M$  so that  $[\bar{p}_t]_i$ , the  $i$ th element of the  
 11  $M \times 1$  (column) vector  $\bar{p}_t$ , is equal to the conditional probability  $\Pr\{s_{t+1} = 0 | s_t = i\}$  for  $1 \leq i \leq M$ .

12 The complete state transition probability matrix is

$$P_t(a_t) = \begin{bmatrix} 1 & \mathbf{0}_M^T \\ \bar{p}_t & \text{diag}[\mathbf{1}_M - \bar{p}_t] \tilde{P}_t(a_t) \end{bmatrix}, \quad (2)$$

13 where  $\mathbf{0}_M$  is the  $M \times 1$  (column) vector of zeros and  $\mathbf{1}_M$  is the  $M \times 1$  (column) vector of ones.

14 *Rewards:* There are many possible reward structures for our model depending on the decision  
 15 maker's perspective. In this article we define rewards to be composed of four parts: (i) a reward for  
 16 quality-adjusted time gained in the most recent period (e.g., a QALY for an annual decision epoch);  
 17 (ii) a cost associated with an adherence intervention; (iii) a state-dependent cost of medication; and  
 18 (iv) a penalty cost for entering the absorbing state. We define  $r_t(s_t, a_t)$  to be the reward accrued

1 in state  $s_t$  given action  $a_t$  is taken. The reward function is defined as

$$r_t(s_t, a_t) = \begin{cases} R \times Q(s_t) - C^{\text{MED}}(s_t) & \text{for } a_t = W \text{ and } s_t = 1, \dots, M, \\ R \times Q(s_t) - C^{\text{MED}}(s_t) - C^{\text{INT}} & \text{for } a_t = I \text{ and } s_t = 1, \dots, M, \\ -C_t^{\text{F}} & \text{for } s_t = 0, \end{cases} \quad (3)$$

2 where  $R$  is the *willingness-to-pay* factor defining a monetary value per QALY and  $Q(s_t)$  represents  
3 the QALYs for a patient in state  $s_t$  during time epoch  $t$ . The quantity  $C^{\text{MED}}(s_t)$  denotes the cost  
4 of medication for time epoch  $t$ ; this cost depends on the patient's adherence state since patients do  
5 not pay for medication they do not have in their possession. The quantity  $C^{\text{INT}}$  denotes the cost  
6 of an adherence-improving intervention. The quantity  $C_t^{\text{F}}$  represents a one-time lump sum for the  
7 expected future costs of a patient entering the absorbing state 0. This cost penalty reflects a loss  
8 associated with failure to avoid an adverse health event. This loss could include costs associated  
9 with hospitalization and/or future treatment. This one-time negative reward occurs upon entering  
10 the absorbing state, and all future rewards for patients in the absorbing state are zero. Thus, the  
11 expected future rewards, or value-to-go, for patients that have just entered the absorbing state is  
12 zero.

13 The reward structure presented above represents a combination of the patient objective of  
14 maximizing quality-adjusted time to first event (which is frequently the clinical intent of preventive  
15 treatment (Cleeman et al. [2001])) and the objective of minimizing costs of treatment, considering  
16 both costs before the patient enters the absorbing state and expected costs after the patient enters  
17 the absorbing state. Additional assumptions about the reward structure are provided in Section  
18 5, and specific values for rewards are provided in Section 6 in the context of cardiovascular disease  
19 prevention.

20 For a patient in state  $s_t \in S$  in epoch  $t$ , the optimality equations can be written as

$$v_t(s_t) = \max_{a_t \in A_t(s_t)} \left\{ r_t(s_t, a_t) + \lambda \sum_{s_{t+1} \in S} p_t(s_{t+1} | s_t, a_t) v_{t+1}(s_{t+1}) \right\}, \text{ for every } t = 1, \dots, T - 1, \quad (4)$$

1 where  $p_t(s_{t+1}|s_t, a_t)$  is the  $(s_t, s_{t+1})$  element of  $P_t(a_t)$ ,  $v_t(s_t)$  is the optimal value function, and  
 2  $\lambda \in [0, 1)$  is the discount factor which calculates the time  $t$  value of rewards received at time  $t + 1$ .  
 3 For every time  $t \in \{0, 1, \dots, T\}$ , we define  $\mu_t(s_t)$  to be the expected difference between the rewards  
 4 for quality-adjusted survival benefits and the associated costs, assuming no future interventions,  
 5 for every  $s_t \in S$ . We take  $\mu_t(0) = -C_t^F$  provided that  $s_{t-1} \neq 0$ , and  $\mu_t(0) = 0$  otherwise. The  
 6 end-of-horizon boundary condition is

$$v_T(s_T) = \mu_T(s_T), \text{ for every } s_T \in S. \quad (5)$$

7 The last decision epoch,  $T$ , is selected to represent a reasonable upper bound on the age at which  
 8 adherence-improving interventions would no longer be advisable due to high competing risks of  
 9 death from other causes. This end-of-horizon assumption has been made in a number of other  
 10 medical decision making studies (Denton et al. [2009], Chhatwal et al. [2010], Kurt et al. [2011]).

## 11 5 Model Properties and Insights

12 This section provides insights into the structure of our model. First, we discuss some of the  
 13 assumptions of our model. Next, we present some properties of our model that can reduce the  
 14 computational effort to solve the MDP, and that provide some insight into the optimal policy for  
 15 interventions defined by our model. We prove the existence of an optimal control limit policy.  
 16 We provide sufficient conditions for optimality of an intervention that could be used in practice  
 17 to determine if an intervention should be undertaken. Next, we present a theorem relating the  
 18 effectiveness of interventions to the optimal control limits for the interventions. Finally, we present  
 19 a theorem comparing the optimal control limits for two patients where one patient is at a greater  
 20 risk for adverse health events than the other.

### 21 5.1 Model Assumptions

22 There are many possible choices for the reward function to use in our MDP model. We chose to  
 23 blend two criteria for our reward function: the patient reward for quality-adjusted time to first  
 24 event and the payer cost of treatment, intervention, and care associated with an adverse health

1 event. We make the following assumptions about our model:

- 2 (i)  $\tilde{P}_t(a_t)$  has the increasing failure rate (IFR) property for every  $a_t \in A$ , and for every  $t \in$   
3  $\{0, 1, \dots, T\}$ ;
- 4 (ii)  $\mu_t(s_t)$  is nondecreasing in  $s_t$ ;
- 5 (iii)  $[\bar{p}_t]_i \equiv \Pr\{s_{t+1} = 0 | s_t = i\}$  is nonincreasing in  $s_t$ ; and
- 6 (iv)  $R \times Q(s_t) - C^{\text{MED}}(s_t)$  is a nondecreasing function of  $s_t$ .

7 Assumption (i) states that the Markov chain defining a patient’s adherence exhibits the IFR prop-  
8 erty (see Barlow and Proshan [1965] for a definition of this property). This can be interpreted to  
9 mean that the better a patient’s adherence level the better it is likely to be in the future. Our  
10 study using observational data (see Section 6) suggests that this is a reasonable assumption. This  
11 property has also been observed for a number of other health characteristics (Alagoz et al. [2004],  
12 Kurt et al. [2011], Chhatwal et al. [2010]). Assumption (ii) states that a patient’s expected future  
13 rewards for QALYs minus costs, assuming no future interventions, does not decrease as their ad-  
14 herence improves. This assumption is reasonable since improved adherence causes treatment to be  
15 more effective at preventing adverse events. Assumption (iii) states that the probability of moving  
16 to the absorbing state is nonincreasing in the adherence state. Finally, assumption (iv) states that  
17 the difference between  $R \times Q(s_t)$ , the reward for living through a decision epoch, and  $C^{\text{MED}}(s_t)$ ,  
18 the cost of medication, is a nondecreasing function of the adherence state  $s_t$ . In addition to the  
19 above assumptions, we assume that  $R, Q(s_t), C^{\text{INT}}, C_t^{\text{F}}$ , and  $C^{\text{MED}}(s_t)$  are nonnegative for every  
20 value of  $s_t$ .

## 21 5.2 Model Properties

22 We now discuss some properties associated with the optimal adherence intervention policy and  
23 draw comparisons between different types of patients and interventions. We begin by presenting  
24 two lemmas that are used to prove our main results.

25 Assumption (i) stated that transitions among adherence states, defined by  $\tilde{P}_t(a_t)$ , are IFR.  
26 Lemma 1 extends this by stating that the complete transition probability matrix,  $P_t(a_t)$ , is IFR



1 if the conditional transition matrix among the adherence states given avoidance of state 0 is IFR.  
 2 We show that if the rows of  $\tilde{P}_t(a_t)$  are in increasing stochastic order, then the rows of  $P_t(a_t)$  must  
 3 also be in increasing stochastic order.

4 **LEMMA 1.** *If  $\tilde{P}_t(a_t)$  is IFR and assumption (iii) holds, then  $P_t(a_t)$  is IFR.*

5 *Proof.* Proof of Lemma 1: Since  $\tilde{P}_t(a_t)$  is IFR by assumption (i), with  $(i, j)$  element  $\tilde{p}_t(j|i, a_t) \equiv$   
 6  $[\tilde{P}_t(a_t)]_{i,j}$ , it follows that for each  $k \in \{1, \dots, M\}$ , the quantity

$$\tilde{q}_t(k|i, a_t) = \sum_{j=k}^M \tilde{p}_t(j|i, a_t) \quad (6)$$

7 is nondecreasing in  $i$  for  $i = 1, \dots, M$ . The matrix multiplication  $\text{diag}[\mathbf{1}_M - \bar{p}_t] \tilde{P}_t(a_t)$  involves  
 8 multiplying the  $i$ th row of  $\tilde{P}_t(a_t)$  through by  $1 - [\bar{p}_t]_i$  for  $i \in \{1, \dots, M\}$ . Therefore, since  $1 - [\bar{p}_t]_i$   
 9 is nondecreasing in  $i$  by assumption (iii), it follows that the  $(M + 1) \times M$  matrix

$$Z \equiv \begin{bmatrix} \mathbf{0}_M^T \\ \text{diag}[\mathbf{1}_M - \bar{p}_t] \tilde{P}_t(a_t) \end{bmatrix} \quad (7)$$

10 with  $(u, v)$  element  $Z_{u,v}$  for  $u \in \{0, 1, \dots, M\}$  and  $v \in \{1, \dots, M\}$  satisfies the following IFR-like  
 11 property: for each fixed  $k \in \{1, \dots, M\}$ , the function

$$z(u) \equiv \sum_{v=k}^M Z_{u,v} \quad (8)$$

12 is nondecreasing in  $u$  for  $u \in \{0, 1, \dots, M\}$ . Finally, we see that  $P_t(a_t)$  is IFR since  $\sum_{j=0}^M p_t(j|i, a_t) =$   
 13 1, for every  $i = 0, \dots, M$ . □

14 The next lemma states that the value function does not decrease as the patient's adherence im-  
 15 proves.

16 **LEMMA 2.** *The value function  $v_t(s_t)$  is nondecreasing in  $s_t$ , for  $t = 1, \dots, T$ .*

17 *Proof.* Proof of Lemma 2: This follows from Proposition 4.7.3 of Puterman [1994] and the fact that  
 18 the following conditions hold:

1     1. The quantity  $r_t(s_t, a_t)$  is nondecreasing in  $s_t$ , for every  $a_t \in A_t(s_t)$ , by assumption (iv) and  
 2     Equation (3).

3     2. For each  $k \in \{0, 1, \dots, M\}$ , the analogue of Equation (6) for the matrix  $P_t(a_t)$ ,

$$q_t(k|s_t, a_t) \equiv \sum_{j=k}^M p_t(j|s_t, a_t) \tag{9}$$

4     is nondecreasing in  $s_t$ , for every  $a_t \in A_t(s_t)$ , by Lemma 1 for  $t = 1, \dots, T - 1$ .

5     3.  $\mu_T(s_T)$  is nondecreasing in  $s_T$  by assumption (ii).

6     □

7     Lemma 2 shows that the patient’s expected future rewards do not decrease as adherence to treat-  
 8     ment improves. This fact is used to prove Theorem 1 which states that the optimal intervention  
 9     policy has a simple control-limit structure for the adherence states  $s_t = 1, \dots, M$ .

10    **THEOREM 1.** *If the effect of an intervention is independent of the patient’s current adherence*  
 11    *state, then there exists an optimal control limit  $s_t^* \in S \setminus \{0\}$ , for every  $t$ , such that the optimal*  
 12    *action  $a_t^*(s_t)$  is given by*

$$a_t^*(s_t) = \begin{cases} I, & \text{if } s_t \leq s_t^*, \text{ for every } s_t \in S \setminus \{0\}, \\ W, & \text{otherwise.} \end{cases} \tag{10}$$

*Proof.* Proof of Theorem 1: We prove the existence of the control-limit policy for the entire set  $S$ , where it is understood that the action for  $s_t = 0$  is defined as  $W$ . If we associate, for example, the numerical value 0 with the action  $W$  and the numerical value 1 with the action  $I$ , then from Theorem 4.7.4 of Puterman (1994) it is sufficient to prove the following: (a)  $r_t(s_t, a_t)$  is nondecreasing in  $s_t$  for all  $a_t \in A_t(s_t)$ ; (b)  $q_t(k|s_t, a_t)$  is nondecreasing in  $s_t$  for all  $k \in S$  and  $a_t \in A_t(s_t)$ ; (c)  $r_t(s_t, a_t)$  is a subadditive function on  $S \times A_t(s_t)$ ; (d)  $q_t(k|s_t, a_t)$  is a subadditive function on  $S \times A_t(s_t)$  for all  $k \in S$ ; and (e)  $\mu_T(s_T)$  is nondecreasing in  $s_T$ . Conditions (a), (b), and (e) follow by assumption (iv), Lemma 1, and assumption (ii), respectively. Condition (c) follows because  $(r_t(s_t + 1, 1) - r_t(s_t + 1, 0)) - (r_t(s_t, 1) - r_t(s_t, 0)) \leq 0$ , for every  $s_t \in S$ . To prove condition (d) we

must show

$$q_t(k|i+1, 1) - q_t(k|i+1, 0) \leq q_t(k|i, 1) - q_t(k|i, 0)$$

for every  $k \in S$  and for every  $s_t \in S$ . In order for the above inequality to be true, the following must also hold

$$\sum_{j=k}^M p_t(j|i+1, 1) - \sum_{j=k}^M p_t(j|i+1, 0) \leq \sum_{j=k}^M p_t(j|i, 1) - \sum_{j=k}^M p_t(j|i, 0),$$

1 which can be expressed as

$$\sum_{j=k}^M p_t(j|i+1, 1) + \sum_{j=k}^M p_t(j|i, 0) \leq \sum_{j=k}^M p_t(j|i, 1) + \sum_{j=k}^M p_t(j|i+1, 0). \quad (11)$$

2 This inequality holds for the first terms on each side of Equation (11) by the assumption that the  
 3 affect of an intervention is independent of the patient's current adherence state. The inequality  
 4 holds for the second terms on each side of Equation (11) by Lemma 1.  $\square$

5 Theorem 1 provides sufficient conditions under which the optimal intervention policy has a  
 6 simple structure, which is important for clinical applications in practice. This structure can also  
 7 be exploited to achieve computational advantages in computing the optimal policy. This could be  
 8 particularly relevant for applications involving real-time clinical intervention decisions.

9 Next we provide an intuitive sufficient condition for optimality of an intervention in a given  
 10 state  $s_t$  at time  $t$ . The following theorem states that it is optimal to perform an intervention if the  
 11 worst case marginal benefit is greater than or equal to the cost of the intervention.

12 **THEOREM 2.** *The following is a sufficient condition for optimality of an intervention in a given*  
 13 *epoch  $t$ :*

$$p_t(0|s_t, W) - p_t(0|s_t, I) \geq \frac{C^{INT}}{\mu_t(1) + C_t^F}. \quad (12)$$

*Proof.* Proof of Theorem 2: It is optimal to perform an intervention in state  $s_t \neq 0$  at epoch  $t$  if

$$\begin{aligned} R \times Q(s_t) - C^{\text{MED}}(s_t) - C^{\text{INT}} + \sum_{s_{t+1}=0}^M p_t(s_{t+1}|s_t, I)v_{t+1}(s_{t+1}) \\ \geq R \times Q(s_t) - C^{\text{MED}}(s_t) + \sum_{s_{t+1}=0}^M p_t(s_{t+1}|s_t, W)v_{t+1}(s_{t+1}). \end{aligned}$$

Therefore, it is optimal if

$$\sum_{s_{t+1}=0}^M (p_t(s_{t+1}|s_t, I) - p_t(s_{t+1}|s_t, W))v_{t+1}(s_{t+1}) \geq C^{\text{INT}}.$$

We can expand the left side of this inequality to the following:

$$\sum_{s_{t+1}=1}^M (p_t(s_{t+1}|s_t, I) - p_t(s_{t+1}|s_t, W))v_{t+1}(s_{t+1}) + (p_t(0|s_t, I) - p_t(0|s_t, W))(-C_t^{\text{F}}) \geq C^{\text{INT}}.$$

Replacing  $v_{t+1}(s_{t+1})$  with the lower bound  $\mu_t(1)$  the above inequality can be written as:

$$(p_t(0|s_t, W) - p_t(0|s_t, I))(\mu_t(1) + C_t^{\text{F}}) \geq C^{\text{INT}}.$$

1

□

2 This condition is most easily interpreted if it is considered from the patient and payer perspec-  
 3 tives separately. From the patient perspective, it is reasonable to assume  $C_t^{\text{F}} = 0$  and  $C^{\text{MED}}(s_t) = 0$ ,  
 4 for every  $s_t$ , where the latter assumption presumes the patient incurs little or none of the cost of  
 5 treatment (this is consistent with many U.S. insurance plans which impose very low copays for stan-  
 6 dard preventive treatments). From the patient perspective,  $\mu_t(1)$  represents the expected quality  
 7 adjusted survival given the worst level of adherence and no future interventions, and  $C^{\text{INT}}$  can be  
 8 interpreted as the disutility of an intervention. Thus, Theorem 2 can be interpreted to mean that  
 9 if the change in the probability of an event is greater than the ratio of disutility of an intervention  
 10 to expected quality adjusted survival, then an intervention is optimal from the patient perspective.

11 From the payer perspective, the condition in Theorem 2, can be interpreted as follows. The  
 12 parameters  $C_t^{\text{F}}$ ,  $C^{\text{MED}}(s_t)$ , and  $C^{\text{INT}}$  are monetary costs for reaching the absorbing state (e.g.,

1 hospitalization and/or the cost of follow-up medical services following an event), for medication,  
 2 and for an intervention, respectively. From the payer perspective,  $\mu_t(1)$  represents the expected  
 3 future costs for the patient given there are no more interventions. Given this interpretation, the  
 4 condition in Theorem 2 can be interpreted to mean that if the change in the probability of an  
 5 event is greater than the ratio of the cost of an intervention to the expected future costs, then an  
 6 intervention is optimal from the payer perspective.

7 In Section 6 we show that the sufficient condition in Theorem 2 motivates a simple heuristic  
 8 for when to perform an intervention.

9 The remainder of this section presents theorems based on the comparison of optimal policies  
 10 for different types of interventions and different types of patients. We begin with a definition of  
 11 stochastic dominance relevant to the two theorems.

**Definition 1.**  $P_1$  is said to stochastically dominate  $P_2$ , denoted by  $P_1 \succcurlyeq P_2$ , if

$$\sum_{j=k}^M P_1(j|i) \geq \sum_{j=k}^M P_2(j|i), \text{ for every } i, k \in S.$$

12 In order to differentiate the control limits for two interventions, we introduce the following  
 13 notation:  $s_t^*(I)$  represents the optimal control limit for intervention  $I$ . In addition, we use a  
 14 superscript to differentiate probabilities and value functions from the two MDPs in the following  
 15 theorem.

16 **THEOREM 3.** Given an MDP with intervention  $I_1$  and a second MDP with intervention  $I_2$ , if the  
 17 two MDPs are identical except  $P_t^{(1)}(I_1) \succcurlyeq P_t^{(2)}(I_2)$ , then  $s_t^*(I_1) \geq s_t^*(I_2)$ .

18 *Proof.* Proof of Theorem 3:

The proof is by contradiction. For any given epoch  $t$ , assume for the MDP with intervention  
 $I_1$  there is a state  $s_t \leq s_t^*(I_2)$  such that

$$\begin{aligned} & R \times Q(s_t) - C^{\text{MED}}(s_t) - C^{\text{INT}} + \sum_{s_{t+1}=0}^M p_t^{(1)}(s_{t+1}|s_t, I_1) v_{t+1}^{(1)}(s_{t+1}) \\ & < R \times Q(s_t) - C^{\text{MED}}(s_t) + \sum_{s_{t+1}=0}^M p_t^{(1)}(s_{t+1}|s_t, W) v_{t+1}^{(1)}(s_{t+1}). \end{aligned}$$

The above inequality simplifies to

$$\sum_{s_{t+1}=0}^M p_t^{(1)}(s_{t+1}|s_t, I_1) v_{t+1}^{(1)}(s_{t+1}) < \sum_{s_{t+1}=0}^M p_t^{(1)}(s_{t+1}|s_t, W) v_{t+1}^{(1)}(s_{t+1}) + C^{\text{INT}}.$$

1 This implies the following two conditions hold simultaneously

2 (1)  $\sum_{s_{t+1}=0}^M (p_t^{(1)}(s_{t+1}|s_t, I_1) - p_t^{(1)}(s_{t+1}|s_t, W)) v_{t+1}^{(1)}(s_{t+1}) < C^{\text{INT}}$ , and

3 (2)  $\sum_{s_{t+1}=0}^M (p_t^{(2)}(s_{t+1}|s_t, I_2) - p_t^{(2)}(s_{t+1}|s_t, W)) v_{t+1}^{(2)}(s_{t+1}) \geq C^{\text{INT}}$ .

Therefore it follows that

$$\begin{aligned} & \sum_{s_{t+1}=0}^M (p_t^{(1)}(s_{t+1}|s_t, I_1) - p_t^{(1)}(s_{t+1}|s_t, W)) v_{t+1}^{(1)}(s_{t+1}) \\ & < \sum_{s_{t+1}=0}^M (p_t^{(2)}(s_{t+1}|s_t, I_2) - p_t^{(2)}(s_{t+1}|s_t, W)) v_{t+1}^{(2)}(s_{t+1}). \end{aligned} \quad (13)$$

4 We will show this is a contradiction (using Lemma 4.7.2 of Puterman) if the following two conditions  
5 hold for all  $t$

6 (a)  $\sum_{s_{t+1}=k}^M (p_t^{(1)}(s_{t+1}|s_t, I_1) - p_t^{(1)}(s_{t+1}|s_t, W)) \geq \sum_{s_{t+1}=k}^M (p_t^{(2)}(s_{t+1}|s_t, I_2) - p_t^{(2)}(s_{t+1}|s_t, W))$ ,

7 for every  $k \in S$ , and

8 (b)  $v_{t+1}^{(1)}(s_{t+1}) \geq v_{t+1}^{(2)}(s_{t+1})$ .

Condition (a) follows from the assumptions that  $P_t^{(1)}(I_1) \succcurlyeq P_t^{(2)}(I_2)$  and  $P_t^{(1)}(W) \equiv P_t^{(2)}(W)$ . The proof of condition (b) is by induction. For the base case  $t = T$ , we have the following

$$v_T^{(1)}(s_T) = \mu_T(s_T) = v_T^{(2)}(s_T).$$

Thus,  $v_T^{(1)}(s_T) \geq v_T^{(2)}(s_T)$ . For the inductive step we assume  $v_{t+1}^{(1)}(s_{t+1}) \geq v_{t+1}^{(2)}(s_{t+1})$ . Now we must show  $v_t^{(1)}(s_t) \geq v_t^{(2)}(s_t)$ . Let  $a_t^{(2)*}(s_t)$  be the optimal action for MDP 2 at time  $t$  for a patient in

state  $s_t$ . It follows that

$$v_t^{(1)}(s_t) \geq r_t(s_t, a_t^{(2)*}(s_t)) + \lambda \sum_{s_{t+1}=0}^M p_t^{(1)}(s_{t+1}|s_t, a_t^{(2)*}(s_t)) v_{t+1}^{(1)}(s_{t+1}) \quad (14)$$

$$\geq r_t(s_t, a_t^{(2)*}(s_t)) + \lambda \sum_{s_{t+1}=0}^M p_t^{(2)}(s_{t+1}|s_t, a_t^{(2)*}(s_t)) v_{t+1}^{(1)}(s_{t+1}) \quad (15)$$

$$\geq r_t(s_t, a_t^{(2)*}(s_t)) + \lambda \sum_{s_{t+1}=0}^M p_t^{(2)}(s_{t+1}|s_t, a_t^{(2)*}(s_t)) v_{t+1}^{(2)}(s_{t+1}) \quad (16)$$

$$= v_t^{(2)}(s_t).$$

1 Inequality (14) follows from the fact that  $v_t^{(1)}(s_t)$ , the optimal value function, is lower bounded by  
 2 the value function for any other policy (in this case the optimal policy for MDP 2). Inequality (15)  
 3 holds by the assumptions that  $P_t^{(1)}(I_1) \succcurlyeq P_t^{(2)}(I_2)$  and  $P_t^{(1)}(W) \equiv P_t^{(2)}(W)$ , and inequality (16)  
 4 holds by the inductive hypothesis. Thus,  $v_t^{(1)}(s_t) \geq v_t^{(2)}(s_t)$  for all  $t$ , and the proof of condition (b)  
 5 is complete.

Now we use conditions (a) and (b) to complete the proof. By Lemma 4.7.2 of Puterman the following inequality holds

$$\begin{aligned} & \sum_{s_{t+1}=0}^M (p_t^{(1)}(s_{t+1}|s_t, I_1) - p_t^{(1)}(s_{t+1}|s_t, W)) v_{t+1}^{(1)}(s_{t+1}) \\ & \geq \sum_{s_{t+1}=0}^M (p_t^{(2)}(s_{t+1}|s_t, I_2) - p_t^{(2)}(s_{t+1}|s_t, W)) v_{t+1}^{(1)}(s_{t+1}), \end{aligned} \quad (17)$$

6 since condition (a) holds and  $v_{i+1}^{(1)}(s_{t+1} + 1) \geq v_{i+1}^{(1)}(s_{t+1})$  by Lemma 2. Finally, the following  
 7 inequality holds

$$\begin{aligned} & \sum_{s_{t+1}=0}^M (p_t^{(2)}(s_{t+1}|s_t, I_2) - p_t^{(2)}(s_{t+1}|s_t, W)) v_{t+1}^{(1)}(s_{t+1}) \\ & \geq \sum_{s_{t+1}=0}^M (p_t^{(2)}(s_{t+1}|s_t, I_2) - p_t^{(2)}(s_{t+1}|s_t, W)) v_{t+1}^{(2)}(s_{t+1}), \end{aligned} \quad (18)$$

8 since condition (b) is true. Therefore

$$\begin{aligned}
& \sum_{s_{t+1}=0}^M (p_t^{(1)}(s_{t+1}|s_t, I_1) - p_t^{(1)}(s_{t+1}|s_t, W))v_{t+1}^{(1)}(s_{t+1}) \\
& \geq \sum_{s_{t+1}=0}^M (p_t^{(2)}(s_{t+1}|s_t, I_2) - p_t^{(2)}(s_{t+1}|s_t, W))v_{t+1}^{(2)}(s_{t+1}).
\end{aligned} \tag{19}$$

1 Thus, we have our contradiction since inequality (19) violates inequality (13). □

2 Theorem 3 can be interpreted as follows. If intervention  $I_1$  is more effective than intervention  
3  $I_2$ , then the optimal control limit for  $I_1$  in MDP 1 should be greater than or equal to the optimal  
4 control limit for  $I_2$  in MDP 2. In other words, under the optimal policy, intervention  $I_1$  would be  
5 implemented for a wider range of adherence states.  $I_1$  may be used for patients in better adherence  
6 states than  $I_2$ .

7 In the next, and final, theorem we use a superscript to index patients in order to compare the  
8 optimal intervention thresholds for two types of patients. The superscript for patient 1 is (1') and  
9 the superscript for patient 2 is (2').

10 **THEOREM 4.** *If  $\tilde{P}_t(I) \succcurlyeq \tilde{P}_t(W)$ , then for two patients that are identical except*

$$[\bar{p}_t^{(1')}]_i \geq [\bar{p}_t^{(2')}]_i, \text{ for every } i = 1, \dots, M \tag{20}$$

11 *and*

$$\mu_T^{(1')}(s_T) \leq \mu_T^{(2')}(s_T), \text{ for every } s_T \tag{21}$$

12 *then  $s_t^{*(1')} \leq s_t^{*(2')}$ .*

13 *Proof.* Proof of Theorem 4: Since  $\tilde{P}_t(a_t)$  is the same for both patients it follows that  $P_t^{(2')}(W) \succcurlyeq$   
14  $P_t^{(1')}(W)$  and  $P_t^{(2')}(I) \succcurlyeq P_t^{(1')}(I)$ . The proof for this theorem is similar to the proof for Theorem 3.

The proof is by contradiction. For any given epoch  $t$ , assume for patient 2 there is a state



$s_t \leq s_t^{(1')*}$  such that

$$\begin{aligned} & R \times Q(s_t) - C^{\text{MED}}(s_t) - C^{\text{INT}} + \sum_{s_{t+1}=0}^M p_t^{(2')}(s_{t+1}|s_t, I) v_{t+1}^{(2')}(s_{t+1}) \\ & < R \times Q(s_t) - C^{\text{MED}}(s_t) + \sum_{s_{t+1}=0}^M p_t^{(2')}(s_{t+1}|s_t, W) v_{t+1}^{(2')}(s_{t+1}). \end{aligned}$$

This simplifies to

$$\sum_{s_{t+1}=0}^M p_t^{(2')}(s_{t+1}|s_t, I) v_{t+1}^{(2')}(s_{t+1}) < \sum_{s_{t+1}=0}^M p_t^{(2')}(s_{t+1}|s_t, W) v_{t+1}^{(2')}(s_{t+1}) + C^{\text{INT}}.$$

1 This implies the following two conditions hold simultaneously

2 (1)  $\sum_{s_{t+1}=0}^M (p_t^{(2')}(s_{t+1}|s_t, I) - p_t^{(2')}(s_{t+1}|s_t, W)) v_{t+1}^{(2')}(s_{t+1}) < C^{\text{INT}}$ , and

3 (2)  $\sum_{s_{t+1}=0}^M (p_t^{(1')}(s_{t+1}|s_t, I) - p_t^{(1')}(s_{t+1}|s_t, W)) v_{t+1}^{(1')}(s_{t+1}) \geq C^{\text{INT}}$ .

Therefore it follows that

$$\begin{aligned} & \sum_{s_{t+1}=0}^M (p_t^{(2')}(s_{t+1}|s_t, I) - p_t^{(2')}(s_{t+1}|s_t, W)) v_{t+1}^{(2')}(s_{t+1}) \\ & < \sum_{s_{t+1}=0}^M (p_t^{(1')}(s_{t+1}|s_t, I) - p_t^{(1')}(s_{t+1}|s_t, W)) v_{t+1}^{(1')}(s_{t+1}). \end{aligned} \quad (22)$$

4 We prove this is a contradiction if the following two conditions hold for all  $t$

5 (a)  $\sum_{s_{t+1}=k}^M (p_t^{(2')}(s_{t+1}|s_t, I) - p_t^{(2')}(s_{t+1}|s_t, W)) \geq \sum_{s_{t+1}=k}^M (p_t^{(1')}(s_{t+1}|s_t, I) - p_t^{(1')}(s_{t+1}|s_t, W))$ ,

6 for every  $k \in S$ , and

7 (b)  $v_{t+1}^{(2')}(s_{t+1}) \geq v_{t+1}^{(1')}(s_{t+1})$ .

8 The proof of condition (a) is as follows. For  $k = 0$ , the inequality holds trivially. For  $k = 1, \dots, M$ ,

9 we have the following

$$\begin{aligned}
& \sum_{s_{t+1}=k}^M (p_t^{(2')}(s_{t+1}|s_t, I) - p_t^{(2')}(s_{t+1}|s_t, W)) \\
&= \sum_{s_{t+1}=k}^M ((1 - [\bar{p}_t^{(2')}]_{s_t})\tilde{p}_t(s_{t+1}|s_t, I) - (1 - [\bar{p}_t^{(2')}]_{s_t})\tilde{p}_t(s_{t+1}|s_t, W)) \\
&= (1 - [\bar{p}_t^{(2')}]_{s_t}) \sum_{s_{t+1}=k}^M (\tilde{p}_t(s_{t+1}|s_t, I) - \tilde{p}_t(s_{t+1}|s_t, W)) \\
&\geq (1 - [\bar{p}_t^{(1')}]_{s_t}) \sum_{s_{t+1}=k}^M (\tilde{p}_t(s_{t+1}|s_t, I) - \tilde{p}_t(s_{t+1}|s_t, W)) \tag{23} \\
&= \sum_{s_{t+1}=k}^M ((1 - [\bar{p}_t^{(1')}]_{s_t})\tilde{p}_t(s_{t+1}|s_t, I) - (1 - [\bar{p}_t^{(1')}]_{s_t})\tilde{p}_t(s_{t+1}|s_t, W)) \\
&= \sum_{s_{t+1}=k}^M (p_t^{(1')}(s_{t+1}|s_t, I) - p_t^{(1')}(s_{t+1}|s_t, W)),
\end{aligned}$$

1 where  $\tilde{p}_t(s_{t+1}|s_t, a_t)$  is the  $(s_t, s_{t+1})$  element of  $\tilde{P}_t(a_t)$ . Inequality (23) follows by the assumptions  
2 that  $[\bar{p}_t^{(1')}]_i \geq [\bar{p}_t^{(2')}]_i$  and  $\tilde{P}_t(I) \succcurlyeq \tilde{P}_t(W)$ .

The proof of condition (b) is by induction. For the base case  $t = T$ , we have the following

$$v_T^{(2')}(s_T) = \mu_T^{(2')}(s_T) \geq \mu_T^{(1')}(s_T) = v_T^{(1')}(s_T).$$

Thus,  $v_T^{(2')}(s_T) \geq v_T^{(1')}(s_T)$ . For the inductive step we assume  $v_{t+1}^{(2')}(s_{t+1}) \geq v_{t+1}^{(1')}(s_{t+1})$ . Now we must show  $v_t^{(2')}(s_t) \geq v_t^{(1')}(s_t)$ . Let  $a_t^{(1')*}(s_t)$  be the optimal action at time  $t$  for patient 1 in state  $s_t$ . It follows that

$$v_t^{(2')}(s_t) \geq r_t(s_t, a_t^{(1')*}(s_t)) + \lambda \sum_{s_{t+1}=0}^M p_t^{(2')}(s_{t+1}|s_t, a_t^{(1')*}(s_t))v_{t+1}^{(2')}(s_{t+1}) \tag{24}$$

$$\geq r_t(s_t, a_t^{(1')*}(s_t)) + \lambda \sum_{s_{t+1}=0}^M p_t^{(1')}(s_{t+1}|s_t, a_t^{(1')*}(s_t))v_{t+1}^{(2')}(s_{t+1}) \tag{25}$$

$$\geq r_t(s_t, a_t^{(1')*}(s_t)) + \lambda \sum_{s_{t+1}=0}^M p_t^{(1')}(s_{t+1}|s_t, a_t^{(1')*}(s_t))v_{t+1}^{(1')}(s_{t+1}) \tag{26}$$

$$= v_t^{(1')}(s_t).$$

1 Inequality (25) holds since  $P_t^{(2')}(W) \succcurlyeq P_t^{(1')}(W)$  and  $P_t^{(2')}(I) \succcurlyeq P_t^{(1')}(I)$ . Thus,  $v_t^{(2')}(s_t) \geq v_t^{(1')}(s_t)$   
2 for all  $t$ , and the proof of condition (b) is complete.

3 Now we use conditions (a) and (b) to complete the proof. By Lemma 4.7.2 of Puterman the  
4 following inequality holds

$$\begin{aligned} & \sum_{s_{t+1}=0}^M (p_t^{(2')}(s_{t+1}|s_t, I) - p_t^{(2')}(s_{t+1}|s_t, W))v_{t+1}^{(2')}(s_{t+1}) \\ & \geq \sum_{s_{t+1}=0}^M (p_t^{(1')}(s_{t+1}|s_t, I) - p_t^{(1')}(s_{t+1}|s_t, W))v_{t+1}^{(2')}(s_{t+1}), \end{aligned} \quad (27)$$

since condition (a) holds and  $v_{t+1}^{(2')}(s_{t+1} + 1) \geq v_{t+1}^{(2')}(s_{t+1})$  by Lemma 2. Finally, the following  
condition holds

$$\begin{aligned} & \sum_{s_{t+1}=0}^M (p_t^{(1')}(s_{t+1}|s_t, I) - p_t^{(1')}(s_{t+1}|s_t, W))v_{t+1}^{(2')}(s_{t+1}) \\ & \geq \sum_{s_{t+1}=0}^M (p_t^{(1')}(s_{t+1}|s_t, I) - p_t^{(1')}(s_{t+1}|s_t, W))v_{t+1}^{(1')}(s_{t+1}), \end{aligned} \quad (28)$$

5 since condition (b) is true. Therefore

$$\begin{aligned} & \sum_{s_{t+1}=0}^M (p_t^{(2')}(s_{t+1}|s_t, I) - p_t^{(2')}(s_{t+1}|s_t, W))v_{t+1}^{(2')}(s_{t+1}) \\ & \geq \sum_{s_{t+1}=0}^M (p_t^{(1')}(s_{t+1}|s_t, I) - p_t^{(1')}(s_{t+1}|s_t, W))v_{t+1}^{(1')}(s_{t+1}). \end{aligned} \quad (29)$$

6 Thus, we have our contradiction since inequality (29) violates inequality (22).  $\square$

7 Theorem 4 states that if patient 1 has a higher probability of moving to an absorbing state  
8 than patient 2, then patient 2 should have interventions in the same or better adherence states  
9 than patient 1. Since  $P_t^{(2')}(I) \succcurlyeq P_t^{(1')}(I)$ , patient 1, the sicker patient, receives less benefit from  
10 interventions than patient 2. Interventions that are optimal for patient 2 with better adherence

1 may not be optimal for patient 1. This theorem provides a simple criterion for sorting patients on  
2 the basis of importance of an intervention, which could be useful for resource constrained settings.

## 3 **6 Case Study: Statin Adherence for Patients with Type 2 Dia-** 4 **betes**

5 In this section we present a case study to illustrate the application of our model to evaluate a hypo-  
6 thetical EHR-based AAS system in the context of preventive treatment for cardiovascular disease.  
7 Specifically, we investigate adherence interventions for statin treatment among patients with type  
8 2 diabetes. Statins are particularly important for patients with diabetes, since these patients are  
9 at two to four times higher risk for stroke and CHD events over patients without diabetes (CDC  
10 [2011]). Furthermore, long-term adherence to statins is known to be poor (Benner et al. [2002],  
11 Mason et al. [2012]).

12 In Section 6.1 we provide our data sources and model parameters. In Section 6.2 we compare  
13 active and inactive surveillance policies using the MDP model described in Section 4. We present  
14 the optimal policies and expected LYs and costs associated with these policies. We also explore the  
15 effects of gender, the patient’s health risk, the cost of an intervention, the willingness-to-pay factor,  
16 and the type of intervention on the optimal policy. Furthermore, we provide results of numerical  
17 experiments using the sufficient conditions for optimality of an intervention, provided in Theorem  
18 2, as the basis for a heuristic for determining when to perform an intervention. We conclude this  
19 section with an estimate of total benefits of AAS to the U.S. diabetes population.

### 20 **6.1 Data and Model Parameter Estimation**

21 The transition probabilities among adherence states were computed from the administrative med-  
22 ical and pharmacy claims data from a large health insurance company that insures patients across  
23 the United States. A cohort of 54,036 diabetes patients from this dataset were identified us-  
24 ing Healthcare Effectiveness Data and Information Set (HEDIS) criteria for diagnosis of diabetes  
25 (HEDIS [2007]). Patients included in the set were required to have five years of continuous enroll-  
26 ment with first encounter dates ranging from January 1995 to June 2004. The PDC by pharmacy

fills, described in Section 2, was used as a proxy for patient adherence rates. Once the PDC was computed for each patient, the transition probabilities were computed by counting the number of patients in each adherence state that transitioned to each adherence state in the next year. The associated effect of statins on the patient’s TC level for each adherence level was derived from this observational data set as well (see Mason et al. [2012] for a detailed description).

The transition probabilities for stroke and CHD events were derived from the United Kingdom Prospective Diabetes Study (UKPDS) risk models (Kothari et al. [2002], Stevens et al. [2001]), and the probabilities for death from other causes were calculated from the Centers for Disease Control and Prevention (CDC) mortality tables (CDC [2007]). The state of the patient’s health (other than their adherence level), which we used to estimate stroke and CHD event probabilities with the UKPDS model, was based on observations from a large cohort of 663 patients receiving treatment for type 2 diabetes at Mayo Clinic, Rochester, MN. Approximately 15,000 measurements of HbA1c (a patient’s average blood sugar over two to three months), blood pressure, and cholesterol were collected between 1997 and 2006 through the Mayo Clinic Diabetes Electronic Management System (DEMS) (Gorman et al. [2000]).

Table 2: Initial hospitalization costs and follow-up events for adverse events.

Parameter	Cost	Citation
Initial Hospitalization for Stroke	\$13,204	NIS [2006]
Initial Hospitalization for CHD	\$18,590	NIS [2006]
Yearly Follow-up for Stroke	\$1664	Thom et al. [2006]
Yearly Follow-up for CHD	\$2576	Thom et al. [2006]

For all of our experiments we assumed a maximum age of  $T = 100$  as the age at which interventions would be discontinued and a discount factor of  $\lambda = 0.97$  which corresponds to a 3% yearly discount rate (Gold et al. [1996]). For the base case, we assumed a willingness to pay of  $R = \$100,000$  (Evans et al. [2004]) and a cost of statins of  $C^{\text{MED}}(s_t) = \$212 \times \delta(s_t)$ , where  $\delta(s_t)$  represents the mean PDC of a patient in adherence state  $s_t$  (Red Book [2009]). The cost of an intervention was estimated to be  $C^{\text{INT}} = \$123$  from a cost-benefit analysis of interventions by Eastaugh and Hatcher [1982] that was inflated to 2009 dollars using the consumer price index method (BLS [2007]). This intervention cost includes clarification of the doctor’s message, family

1 member reinforcement, and group meetings to improve patient adherence. The initial and follow-up  
 2 costs of stroke and CHD events were drawn from sources in the health services research literature  
 3 provided in Table 2. The one-time penalty of entering the absorbing state,  $C_t^F$ , is computed with  
 4 a Markov chain using these costs and probabilities governing patient survival.

5 The adherence states used in the numerical experiments are NON ( $0 \leq \text{PDC} \leq 10\%$ ), LOW  
 6 ( $10 < \text{PDC} \leq 40\%$ ), MED ( $40 < \text{PDC} \leq 80\%$ ), and HIGH ( $80 < \text{PDC} \leq 100\%$ ) (Mason et al.  
 7 [2012]). The transition probability matrices,  $\tilde{P}_t(a_t)$ , were estimated to be

$$8 \quad \tilde{P}_t(W) = \begin{array}{c} \text{NON} \\ \text{LOW} \\ \text{MED} \\ \text{HIGH} \end{array} \begin{array}{c} \text{NON} \quad \text{LOW} \quad \text{MED} \quad \text{HIGH} \\ \left( \begin{array}{cccc} 0.787 & 0.106 & 0.082 & 0.025 \\ 0.498 & 0.205 & 0.213 & 0.084 \\ 0.199 & 0.154 & 0.390 & 0.257 \\ 0.028 & 0.046 & 0.189 & 0.737 \end{array} \right),$$

9 and

$$10 \quad \tilde{P}_t(I) = \begin{array}{c} \text{NON} \\ \text{LOW} \\ \text{MED} \\ \text{HIGH} \end{array} \begin{array}{c} \text{NON} \quad \text{LOW} \quad \text{MED} \quad \text{HIGH} \\ \left( \begin{array}{cccc} 0.091 & 0.165 & 0.257 & 0.487 \\ 0.091 & 0.165 & 0.257 & 0.487 \\ 0.091 & 0.165 & 0.257 & 0.487 \\ 0.091 & 0.165 & 0.257 & 0.487 \end{array} \right).$$

11 The matrix  $\tilde{P}_t(I)$  was estimated based on the proportion of patients occupying each of the ad-  
 12 herence states in their first year of treatment. This assumption was made since an intervention  
 13 may act to “reset” a patient’s adherence level to the level it was when the patient initially began  
 14 treatment. In addition, we considered the more optimistic case that a patient moves to state HIGH  
 15 with probability 1. Use of this intervention provides a conservative estimate of the improvement  
 16 achievable through interventions.

## 6.2 Numerical Results

Numerical experiments were conducted to find the optimal policy for adherence-improving interventions based on the above model parameters. The model was solved using backwards recursion, implemented in C/C++. Each experiment took less than ten seconds to run using a 2.83GHz PC with 8GB of RAM. Experiments were run for males and females, starting at age 40, assuming a variety of different risk states and different intervention cost estimates. The perfect and imperfect interventions described in Section 6.1 were both evaluated. We represent different risk states by the patient’s TC and high-density lipoprotein (HDL), also known as “good” cholesterol, each given as one of low ( $L$ ), medium ( $M$ ), high ( $H$ ), and very high ( $V$ ). These are the most significant metabolic factors influencing a patient’s risk of stroke or CHD events according to the UKPDS model. While there are a total of 16 patient risk states defined by clinically-relevant thresholds (Cleeman et al. [2001]), for brevity we provide policies and numerical results for representative patients with low risk (low TC and very high HDL), medium risk (medium TC and medium HDL), and high risk (very high TC and low HDL).

### 6.2.1 Active vs. Inactive Surveillance

To estimate the potential benefits of using EHRs to improve adherence to medication at the population level we compared the expected LYs from age 40 prior to an event or death and the expected discounted total costs comprising the costs of intervention, statin treatment, and hospitalizations and follow-up care for CHD events and stroke found using the optimal AAS policy and the IAS policy. IAS involves periodic interventions that do not rely on a patient’s adherence level. We considered interventions that occur every  $k$  years ( $k = 1, 2, 3, 4, \text{ or } 5$ ) after a patient begins taking medication, regardless of the patient’s adherence state. The IAS policy is useful for comparison since it requires no pharmacy or laboratory data and is therefore much easier to implement in practice. We also considered the use of no interventions.

Figures 2 and 3 show the expected LYs vs. costs for AAS, IAS, and no treatment, for females and males. Imperfect interventions were used for these results. We evaluated different AAS policies by varying the willingness-to-pay factor from  $R = \$0$  to  $R = \$1,000,000$ . When the willingness-to-pay factor is varied, different weights are placed on LYs and costs. As this factor increases, a

Figure 2: Comparison of expected LYs verses costs for medication, interventions, and treatment of events for active adherence surveillance (AAS) policies (with varying  $R$  values) and inactive adherence surveillance (IAS) policies (when interventions occur every  $k$  years) for female patients using imperfect interventions. Results are a weighted average of LYs and costs for the 16 possible risk states.

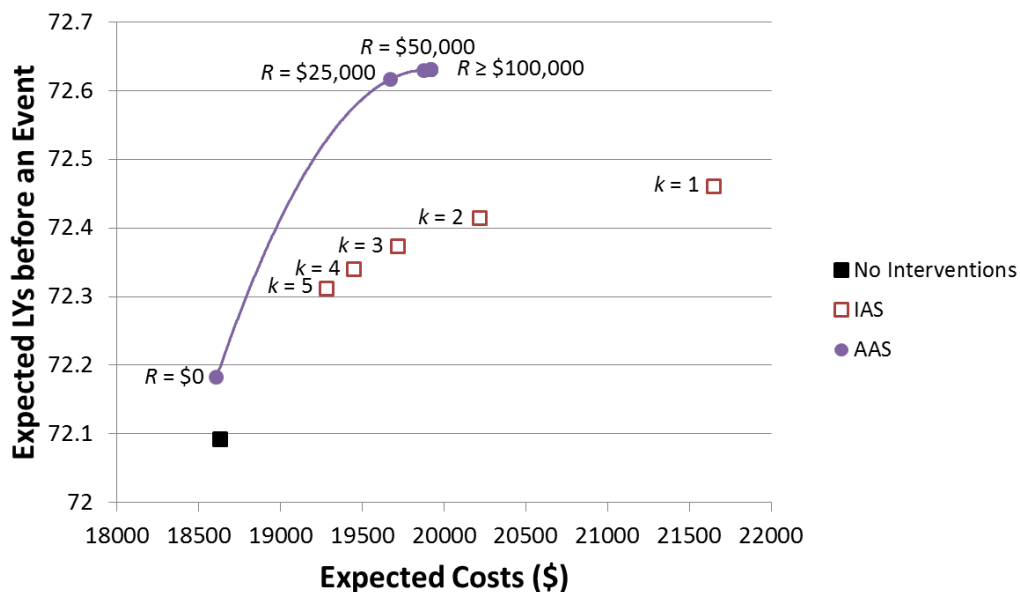
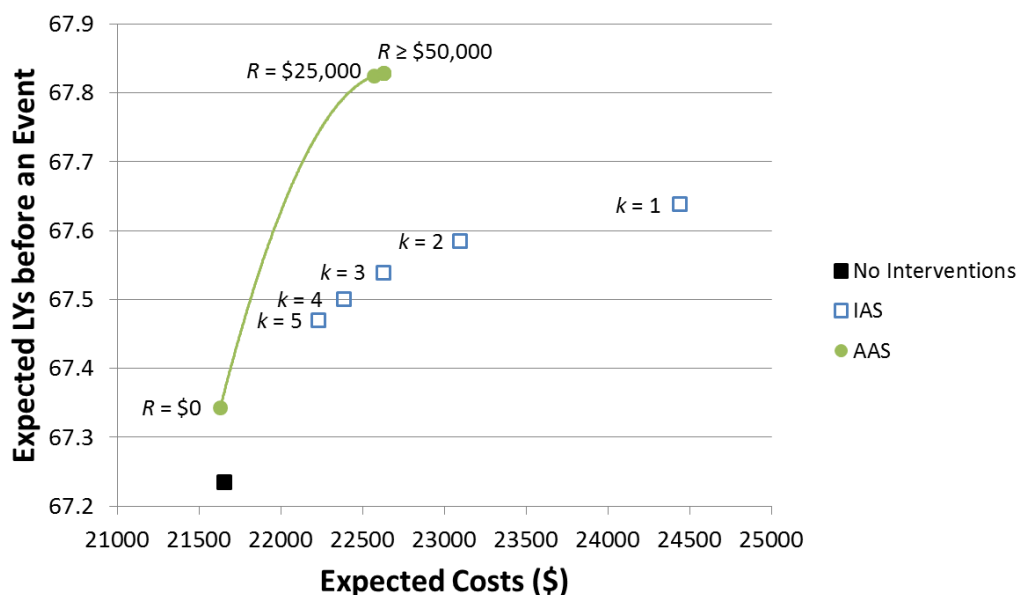


Figure 3: Comparison of expected LYs verses costs, as shown in Figure 2, for male patients.





1 larger weight is placed on maximizing the patient’s LYs rather than minimizing costs. We observe  
2 that AAS outperforms IAS, for females and males, yielding greater expected LYs before an event  
3 or death and lower expected costs when  $R \geq \$25,000$ . When  $R = \$100,000$ , the base case value  
4 for our experiments, the average female patient using AAS receives an expected 0.17 additional  
5 LYs with a \$1727 reduction in costs over IAS ( $k = 1$ ), and the average male patient using AAS  
6 receives an expected 0.19 additional LYs with a \$1808 reduction in costs over IAS ( $k = 1$ ). AAS  
7 resulted in no interventions for patients with HIGH adherence. The higher expected costs incurred  
8 by IAS are presumably due in part to unnecessary interventions for patients with HIGH adherence  
9 to treatment, highlighting the benefit of AAS. It is particularly interesting that there are major  
10 gender differences in the expected LYs before an event or death. Based on our results, we observe  
11 that males are expected to have an adverse event or death approximately 5 years earlier than  
12 females.

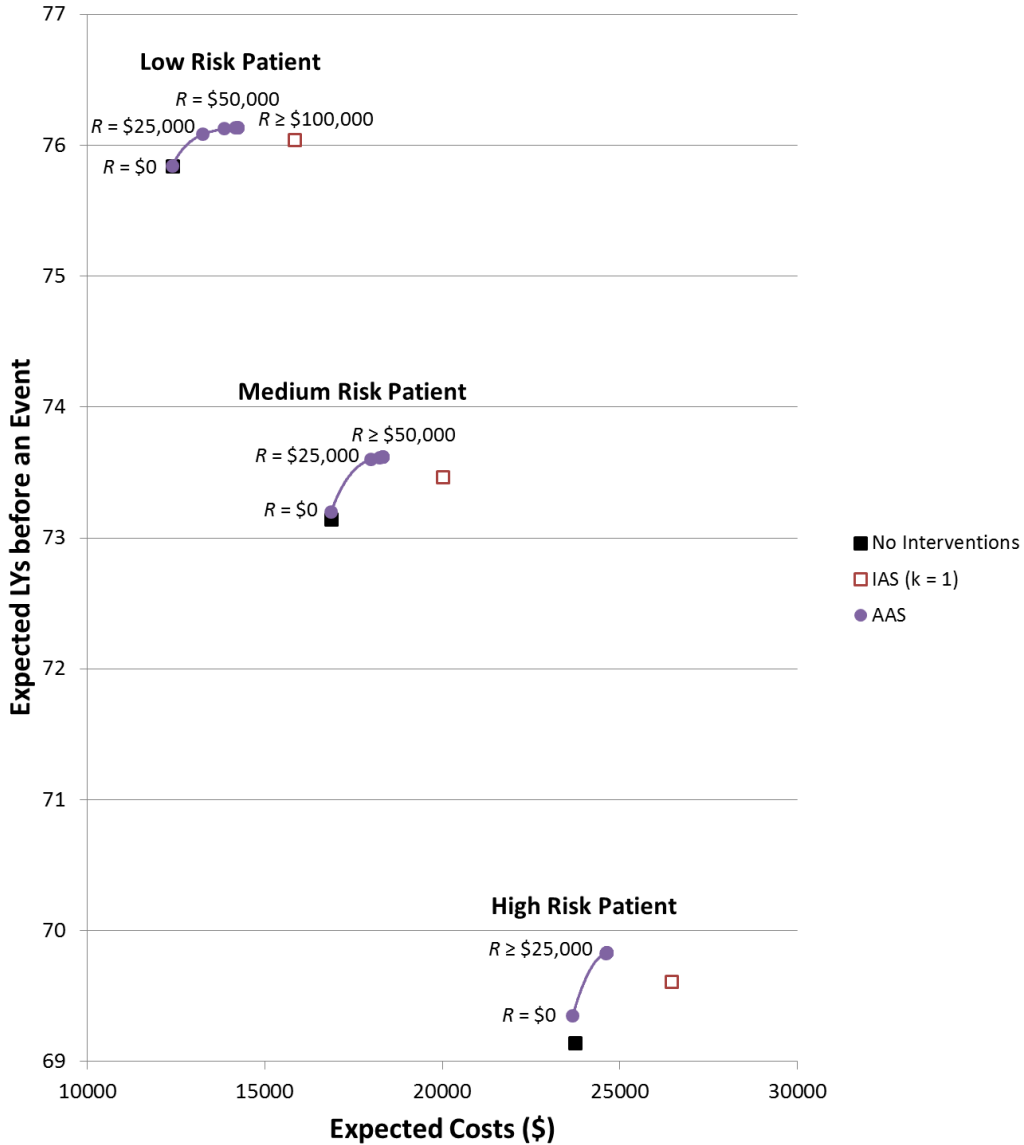
13 While AAS dominates IAS for all 16 risk states, there are significant differences in the magnitude  
14 of the differences in expected cost and LYs for patients with different risk of CHD events and stroke.  
15 Figure 4 presents results for females with low, medium, and high risk in a format similar to Figure  
16 2. Patients with low risk can expect to have their first event or death later in life than patients  
17 with medium or high risk. Also, as a patient’s risk increases, her benefit over no treatment and  
18 her benefit over IAS increases. Thus, it appears the benefit of AAS is increasing in patient risk.  
19 We also note that the expected costs and LYs are less sensitive to changes in the willingness-to-pay  
20 factor as risk increases. The observations for males are consistent with the results for females.

21 We performed sensitivity analysis on the type of intervention. When a perfect intervention is  
22 considered, AAS ( $R = \$100,000$ ) and IAS ( $k = 1$ ) achieve nearly the same expected LYs before  
23 an adverse health event or death, with AAS providing 0.0016 fewer LYs for females and 0.000024  
24 fewer LYs for males. AAS results in an average reduction in costs of \$516 for females and \$635 for  
25 males. Thus, if perfect interventions were achievable, the benefit of AAS would be diminished.

## 26 **6.2.2 Sensitivity to Cost of Intervention**

27 We performed sensitivity analysis on the cost of interventions. When interventions are free, we  
28 observe that patients should have yearly interventions starting at age 41 ( $t = 1$ ), the earliest possible

Figure 4: Comparison of expected LYs verses costs for medication, interventions, and treatment of events for active adherence surveillance (AAS) policies (with varying  $R$  values) and yearly in-active adherence surveillance (IAS) for female patients using imperfect interventions. Results are compared for low, medium, and high risk patients.



age for interventions to occur in our model, since there is no downside for free interventions. For  $C^{\text{INT}} = \$61.50, \$123, \text{ or } \$246$ , we observe female patients should have yearly interventions starting at the ages listed in Tables 3 and 4. The optimal policy for male patients follows a similar pattern to the optimal policy for female patients, but male patients should start having interventions up to 10 years earlier than female patients, depending on the type and cost of intervention. The differences between the policies for male and female patients are likely due to the fact that males generally have an earlier onset of risk for cardiovascular events than females.

The optimal policy, presented in Tables 3 and 4, exhibits a control limit structure, as expected from Theorem 1. We also observe that the control limit tends to increase with respect to age with the exception that at very old ages interventions are no longer optimal. The latest age of intervention ranges from 95 to 98, depending on the patient’s risk level and the cost of the intervention. We expect this is due to the end of horizon approximation in which we truncate the decision horizon at  $T = 100$ .

### 6.2.3 Sensitivity to Individual Patient Risk Factors

In general, female patients and patients with lower risk stop having interventions earlier due to lower risk of stroke and CHD events. The policies are very insensitive to changes in the cost of interventions, particularly for males and patients in higher risk states. We observe that the higher cost interventions have a shorter range for which it is optimal to perform the interventions; that is, the interventions start later and do not continue as late in life. The female patients have fewer interventions overall, with interventions starting later and ending earlier. This is likely due to the

Table 3: Optimal ages to begin having yearly interventions for female patients using active surveillance. Imperfect (probabilistic) interventions are assumed. Note: ‘-’ denotes it is never optimal for the patient to have interventions.

	Low Risk			Medium Risk			High Risk				
	\$61.50	\$123	\$246	\$61.50	\$123	\$246	\$61.50	\$123	\$246		
NON	41	41	41	NON	41	41	41	NON	41	41	41
LOW	41	41	41	LOW	41	41	41	LOW	41	41	41
MED	41	43	54	MED	41	41	42	MED	41	41	41
HIGH	-	-	-	HIGH	-	-	-	HIGH	-	-	-

1 fact that being male is a risk factor for stroke and CHD events, the events statins help prevent.

2 When perfect interventions are considered, it is always optimal for male and female patients  
 3 to have interventions when their adherence is less than HIGH. The use of perfect interventions  
 4 for patients with HIGH adherence depends on the intervention cost and risk state. For imperfect  
 5 interventions, however, patients with HIGH adherence should never have an intervention since the  
 6 probability of remaining in the HIGH adherence state under an intervention is lower than the  
 7 probability of remaining in the HIGH adherence state without an intervention.

#### 8 **6.2.4 Heuristic for Timing of Interventions**

9 We used the sufficient condition provided in Theorem 2 as a heuristic for determining if a patient  
 10 should have an intervention. For this experiment we considered imperfect interventions and the  
 11 base case values for all parameters. If Equation (12) is satisfied, a patient is given an intervention;  
 12 otherwise, no intervention is provided. Compared to the AAS results with  $R = \$100,000$ , the  
 13 average patient receiving interventions based on the heuristic achieves nearly the same expected  
 14 LYs before an adverse health event or death (the expected LYs is exactly the same for males  
 15 and 0.00026 more for females). Compared to the optimal policy, the use of the heuristic costs an  
 16 additional \$239 for the average female patient and an additional \$510 for the average male patient.  
 17 The relative difference between the expected future rewards from age 40 found using the optimal  
 18 policy and found using the heuristic is 0.013% for females and 0.029% for males. In Table 5 we  
 19 provide the relative differences for low, medium, and high risk patients using three different costs  
 20 of interventions. These results show that there is an increasing trend in the relative difference as  
 21 the cost of an intervention increases. For males there also appears to be an increase in the relative

Table 4: Optimal ages to begin having yearly interventions for female patients using active surveillance. Perfect interventions are assumed.

	Low Risk			Medium Risk			High Risk				
	\$61.50	\$123	\$246	\$61.50	\$123	\$246	\$61.50	\$123	\$246		
NON	41	41	41	NON	41	41	41	NON	41	41	41
LOW	41	41	41	LOW	41	41	41	LOW	41	41	41
MED	41	41	41	MED	41	41	41	MED	41	41	41
HIGH	43	55	66	HIGH	41	43	54	HIGH	41	41	41

1 difference as the patient’s risk increases. For females this trend is only evident when  $C^{\text{INT}} = \$246$ .  
 2 Overall, the heuristic appears to be quite effective. Its accuracy decreases marginally as patient  
 3 risk and the cost of intervention increase.

Table 5: Relative difference of the value-to-go from age 40 between use of the optimal treatment policy and the heuristic policy.

	Males			Females		
	$C^{\text{INT}} = \$61.50$	$C^{\text{INT}} = \$123$	$C^{\text{INT}} = \$246$	$C^{\text{INT}} = \$61.50$	$C^{\text{INT}} = \$123$	$C^{\text{INT}} = \$246$
Low Risk	0.010%	0.017%	0.039%	0.006%	0.014%	0.027%
Medium Risk	0.014%	0.025%	0.046%	0.006%	0.012%	0.036%
High Risk	0.020%	0.039%	0.075%	0.008%	0.014%	0.044%

#### 4 6.2.5 Potential Yearly Benefits of AAS to the U.S. Diabetes Population

5 In order to estimate the benefits of AAS applied to all diabetes patients in the United States,  
 6 we first estimated the prevalence of diabetes in the United States using population estimates, by  
 7 age and gender, based on the 2010 U.S. Census (U.S. Census Bureau [2011]), and the estimated  
 8 diabetes prevalence by state and age range reported by Danaei et al. [2009]. Next, we estimated  
 9 the number of newly diagnosed diabetes patients for each gender, for every state and the District  
 10 of Columbia, and for each age, starting at age 40. Patients were defined as *newly diagnosed* in 2010  
 11 if they were a diabetes patient at age 40 or an older patient diagnosed later in life. Patients were  
 12 identified as newly diagnosed past age 40 if the population of total patients diagnosed at earlier ages  
 13 was less than the diagnosed population at the given age. This accounts for increases in population  
 14 and diabetes prevalence with respect to age.

15 Table 6 provides a yearly estimate of expected LYs and costs over the remaining years of life for  
 16 newly diagnosed diabetes patients aged 40 or older with no interventions, IAS ( $k = 1$ ), and AAS.  
 17 According to our model, the implementation of IAS ( $k = 1$ ), compared to no interventions, would  
 18 increase LYs for the U.S. population at a cost of \$6990/LY. In comparison, AAS would increase  
 19 LYs over no interventions for the U.S. population at a cost of \$1455/LY. Using AAS in place of IAS  
 20 ( $k = 1$ ) would result in over 131,000 additional LYs among adults newly diagnosed with diabetes  
 21 while saving over \$1.41 billion per year.

Table 6: Yearly costs (billions) and future LYs for newly-diagnosed diabetes patients using no adherence interventions, yearly inactive adherence surveillance (IAS,  $k = 1$ ), and active adherence surveillance (AAS).

	Males		Females		Total Population	
	LYs	Cost (billions)	LYs	Cost (billions)	LYs	Cost (billions)
No Interventions	8,142,611	\$10.59	10,355,836	\$10.19	18,498,448	\$20.78
IAS ( $k = 1$ )	8,287,353	\$11.53	10,501,173	\$11.28	18,788,525	\$22.81
AAS	8,353,550	\$10.83	10,565,978	\$10.56	18,919,528	\$21.39

## 7 Conclusions

The CMS Meaningful Use initiative has the potential to encourage improved efficiency and effectiveness of healthcare delivery through the use of EHRs. Based on our results we found that the use of EHRs to improve adherence has the potential to significantly delay the onset of adverse events or death, and reduce expected costs of treatment, hospitalization, and follow-up care associated with adverse events such as stroke and CHD. From the population perspective, we found that AAS is cost effective compared to no interventions at a cost of \$1455 spent per LY added prior to CHD, stroke, or death. This cost per LY added is very low with respect to commonly used thresholds (Evans et al. [2004]). In addition, AAS results in significant cost savings over IAS ( $k = 1$ ) while providing more than 131,000 additional event-free LYs to newly diagnosed diabetes patients each year at a savings of \$1.41 billion per year. These estimated annual benefits highlight the potential benefits of AAS. Our study considers the use of AAS for a subpopulation in the United States that is at a high risk of stroke and CHD events; however, AAS could be used for the broader U.S. population and for patients on other medications, yielding additional savings.

From the individual patient perspective, males receive an average of 0.19 additional LYs before an event or death over IAS ( $k = 1$ ) at a reduction in costs of \$1808, and females receive 0.17 additional LYs at a cost savings of \$1727 over IAS ( $k = 1$ ). These increases in LYs over IAS ( $k = 1$ ) are an order of magnitude greater than the benefits seen through some prevention programs that are part of standard practice in the United States. For example, childhood vaccination against measles, mumps, and rubella results in an increase of 0.017 LYs (Wright and Weinstein [1998]). In addition, the increase in LYs from AAS over no interventions is even greater. The benefits of AAS

1 over IAS and no interventions increase with increasing patient risk. In other words, patients at  
2 higher risk of adverse events stand to have greater benefit from AAS.

3 We found the optimal policy for adherence-improving interventions to exhibit a control-limit  
4 type policy. This is consistent with the theoretical results we presented. From our numerical  
5 experiments, it appears that the control limit is increasing with respect to age. Once a patient  
6 begins having interventions, it is generally optimal to continue having yearly interventions until  
7 very late in life. Such a simple policy is encouraging for the application of AAS system in the  
8 already complex clinical environment. We also provided a sufficient condition for an intervention  
9 to be optimal that could be applied as a heuristic at the point of care to decide when an intervention  
10 should occur. Our evaluation of a heuristic based on this condition resulted in the value function  
11 at age 40 differing by less than 0.1% of the optimal value function.

12 We proved structural properties related to the optimal control limit when interventions of  
13 different effectiveness are considered, and when patients of different levels of risk are considered.  
14 While we presented Theorems 3 and 4 in the context of the problem we are applying our model  
15 to (the optimal timing of adherence-improving interventions for patients with type 2 diabetes),  
16 these theoretical properties and our model are generalizable to other contexts. For example, in the  
17 context of machine maintenance, Theorem 4 could be useful in scheduling maintenance for different  
18 types of machines that have different levels of reliability.

19 Although the outcomes of the AAS policy dominated the easier-to-implement IAS outcomes,  
20 our model did not account for the possibility of initial set-up costs and ongoing maintenance costs  
21 for such a system. While the data our model is based on is generally available in administrative  
22 claims systems and laboratory information systems, the development of a decision support system  
23 that collects and utilizes the data would have some cost associated with instantiation of the system  
24 in a clinical environment. Although we did not consider this in our analysis, it is worth noting that  
25 our model can easily be modified to incorporate any maintenance costs that would be necessary to  
26 use AAS. In addition, our model could be used to estimate the payback time for the initial costs  
27 of the system by calculating expected return on investment of using AAS over IAS. Furthermore,  
28 CMS incentives for participation in the Meaningful Use program may offset some of the costs of  
29 implementation.

1        There are some practical challenges associated with the use of EHR data for applications such  
2 as we discuss. First, patients do not always stay with the same insurance provider. There may be  
3 a limited amount of time for which there is continuous information for each patient. This challenge  
4 may eventually be overcome by the development of a universal EHR. Second, our model assumes  
5 population level data can be used to estimate parameters for individual patients. In the case of  
6 adherence to medical treatments, such as statin therapy, this is reasonable because researchers  
7 have not been able to identify ways to predict adherence on the basis of available health data.  
8 Nevertheless, the use of population level data represents a barrier to more accurate prediction of  
9 adherence that might be possible with additional data. Third, in order for AAS to be implemented  
10 at the point of care, EHRs will need to collect and compute patient information such as PDC for  
11 prescribed medications (to estimate the patients adherence level) and patient health information  
12 (such as blood pressure and cholesterol) to estimate the risk of adverse events. While we have  
13 demonstrated this is possible in this article, the ability to rapidly collect and combine such data  
14 presents a challenge for some health systems.

15        Future research could build off of our model in several ways. For example, we considered inter-  
16 ventions for a single medical treatment. Future studies could extend the current model to include  
17 the optimal timing of interventions for patients on multiple medications. This generates a num-  
18 ber of interesting questions. For example, would there be correlations between interventions? In  
19 other words, could an intervention for one medication influence adherence to another medication?  
20 Could an intervention be designed that would simultaneously improve adherence to multiple med-  
21 ications? Furthermore, interesting questions arise about the relative importance of interventions.  
22 For example, our model could be amended to help prioritize interventions for different medications.  
23 Additional variations on our proposed model could include different assumptions about the effec-  
24 tiveness of interventions. Although there is no evidence at present, it is possible that interventions  
25 may provide diminishing improvement to adherence over time. As we pointed out in the intro-  
26 duction, the recent substantial commitment of resources and efforts by the medical community to  
27 improve the current state of knowledge about medication adherence presents a number research  
28 opportunities for the OR community. Our model lays the foundation for some of these future  
29 studies.



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